

Emptiness problem

- Given G , $T_m(G) = \emptyset$?



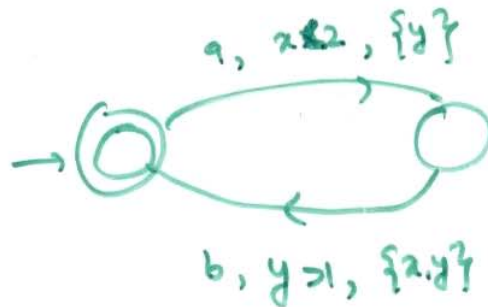
Marked activity state reachable
yet $T_m(G) = \emptyset$.

- Given $T \subseteq (\Sigma \times \mathbb{R}_+^*)$ define

$$\text{untime}(T) \subseteq \Sigma^*$$

to be lang. obtained by projecting
timed traces of T onto Σ^* (by ignoring event occurrence times)

Example:



$$\text{untime}[T_m(G)] = (ab)^*$$

- Lemma: $T = \emptyset$ iff $\text{untime}(T) = \emptyset$.

\Rightarrow Suffices to check emptiness of $\text{untime}(T)$

- Construct an untimed automaton R , called region automaton,
such that $L_m(R) = \text{untime}(T_m(G))$

- Important result (Alur & Dill, '91): R finite state machine

\Rightarrow emptiness of $L_m(R)$ can be verified.