

EE 590F, Homework #2, Fall 2008, Due Friday September 26, 5:00 pm

1. Below are pairs of cost functions and utility functions.

- $C(P)=0.5P^2$ and $U(m,P)=m+\ln(P)$
- $C(P)=e^P$ and $U(m,P)=m+2\sqrt{P}$
- $C(P)=0.5P^4$ and $U(m,P)=m+2P(10-P)$

For each pair,

- Find and draw the corresponding supply and demand functions for P
 - Calculate the competitive equilibrium of the market
 - Check that the competitive allocation maximizes the social surplus
2. The department of Electrical and Computer Engineering at Iowa State University recently received an allocation of 3 parking permits for a highly desirable nearby lot, so that the department can sell the permits to staff members and then do with the money whatever it pleases. There are 6 staff members that want the spaces, but they have different willingness to pay, and different seniorities, according to the below.

Staff member	Willingness to pay	Number of years employed
1	200	10
2	190	12
3	180	15
4	180	14
5	160	16
6	150	5

- If the department allocated the permits according to the competitive equilibrium, what would the equilibrium price and quantity be?
 - Who would buy the permits and who would not?
 - What would the consumer surplus be for each staff member?
 - What would the revenues accrued to the department be?
 - What would happen to the equilibrium if the university decided to tax the permits holders \$5 per permit? Will the staff members be hurt by such a measure? Will the department's revenues change as a result?
3. Continuing problem 2, it was argued that the competitive equilibrium shows no respect for seniority, and further, the competitive price is too high. As a result, the department decided to lower the price of a parking permit to \$100 and to allocate them according to seniority: staff with more seniority have priority; if a "younger" staff member wants a parking permit, s/he should wait until a more senior staff member holding a permit retires.
- What staff members will get a permit?
 - What is the consumer surplus of each of the staff members?
 - Find a mutually beneficial trade between a permit holder & a permitless staff member.
 - Does the new seniority-based allocation mechanism result in an efficient allocation of permits?

4. Consider an electricity market on an island nation with 2 regions: North & South. Relevant data is below, with supply quantities given by q_N and q_S and demand quantities given by x_N and x_S , and all four of them given in per-unit (pu)-hour.
- Cost function for Northern generators: $C_N(q_N) = q_N^2/2$
 - Cost function for Southern generators: $C_S(q_S) = 4q_S + q_S^2/2$.
 - Utility function for Northern consumers: $U_N(m_N, x_N) = m_N + 0.5(200 - x_N)x_N$
 - Utility function for Southern consumers: $U_S(m_S, x_S) = m_S + 0.5(100 - x_S)x_S$
- a. Obtain expressions for the demand and supply functions of the economic agents in each region.
 - b. Assume the Northern and Southern systems are not connected. Draw the Northern and Southern supply-demand curves on separate plots, side-by-side, and identify their respective competitive equilibria.
 - c. Assume there is an infinite capacity transmission line that connects the two regions.
 - i. Set up the appropriate constrained maximization problem, write down the first-order conditions, and find the solution.
 - ii. What is the value(s) of the Lagrange multiplier(s) at the optimum?
 - iii. What is the flow of power that is transmitted along the line? In what direction does power flow?
 - iv. Find the competitive equilibrium. What is the equilibrium price?
 - v. Draw the Northern and Southern supply-demand curves on separate plots, side-by-side, and show the solution obtained in (iv) on both plots.
 - d. Assume the transmission line connecting the two regions has capacity of 16 pu. Answer the same questions i-v as in part c.
5. The paper by Blumsack, Ilic, and Lave, which is downloadable from the website, describes a “stylized example” in Section III. In addition to the information provided in this section of the paper, you can use the following:
- $b_{12} = b_{34} = -10$, $b_{13} = b_{24} = -5$, $b_{23} = -5$
 - The two cost curves, which are

$$C(P_{G1}) = 200 + 10.3P_{G1} + 0.009P_{G1}^2, C(P_{G4}) = 300 + 50P_{G4} + 0.1P_{G4}^2$$
 can be linearized by differentiating them. The constant terms arising in the derivatives will have no effect on the solution and so can be dropped.
- a. Modify the matlab code provided to you in the notes to compute the LMPs with circuit 2-3 out of service. Identify all network LMPs.
 - b. Add circuit 2-3 and recompute the LMPs.
 - c. Do your results agree with what is stated in the paper?
6. Another cap and trade system has been implemented and is described at www.rggi.org/home. Use information at this site to answer the following questions:
- a. What type of emissions does it address?
 - b. When did the effort to develop this cap and trade system begin?
 - c. Who administers the emissions regulations?
 - d. How can power plant owners legally increase undesirable emissions?
 - f. What kind of penalty is associated with violating emissions requirements (\$/ton)?