

## Transmission Line Design Information

In these notes, I would like to provide you with some background information on AC transmission lines.

### 1. AC Transmission Line Impedance Parameters

AC transmission is implemented entirely as 3-phase systems. Initial planning studies typically only consider balanced, steady-state operation. This simplifies modeling efforts greatly in that only the positive sequence, per-phase transmission line representation is necessary.

Essential transmission line electrical data for balanced, steady-state operation includes:

- Line reactance
- Line resistance
- Line charging susceptance
- Current rating (ampacity)
- Surge impedance loading

Figures 1a and 1b below illustrate a *distributed parameter model* of a transmission line where  $z=r+jx$  is the series impedance per unit length (ohms/unit length), and  $y=jb$  is the shunt admittance per unit length (mhos/unit length).

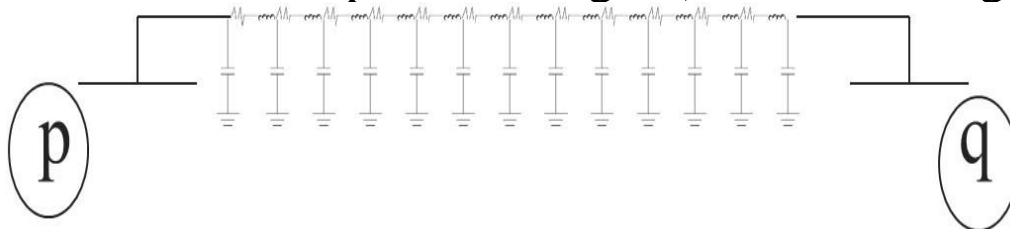


Fig. 1a: Distributed parameter model - conceptual view

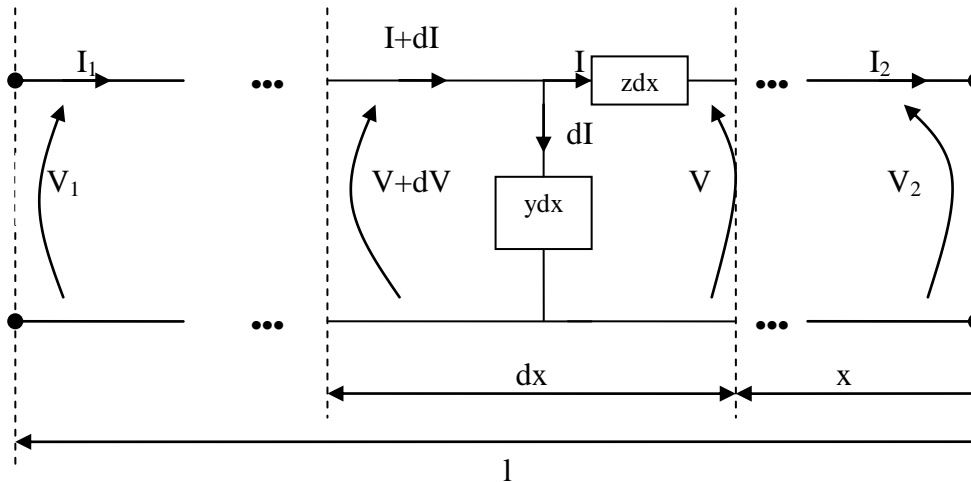


Fig. 1b: Distributed parameter model – analytic view  
 I have notes posted under the lecture for 9/13, at <http://home.engineering.iastate.edu/~jdm/EE456/ee456schedule.htm>, (called “TerminalRelations”) that derive the following model relating voltages & currents at either end of a line.

$$I(l) = I_1 = I_2 \cosh \gamma l + \frac{V_2}{Z_C} \sinh \gamma l \quad (1a)$$

$$V(l) = V_1 = V_2 \cosh \gamma l + Z_C I_2 \sinh \gamma l \quad (1b)$$

where

- $l$  is the line length,
- $\gamma$  is the propagation constant, in general a complex number, given by

$$\gamma = \sqrt{zy} \quad \text{with units of } 1/(\text{unit length}), \quad (1c)$$

where  $z$  and  $y$  are the per-unit length impedance and admittance, respectively, as defined previously.

- $Z_C$  is the characteristic impedance, also known as the surge impedance, given by

$\gamma$  is the propagation constant and is complex, so we can write  $\gamma = \alpha + j\beta$  where  $\alpha$  is the attenuation constant and  $\beta$  is the phase constant. If  $\beta$  is expressed in rad/m, then the wavelength is given by  $\lambda = 2\pi/\beta$  meters. We also have that the wave's velocity of propagation,  $v$ , is close to the speed of light,  $3 \times 10^8$  m/sec, so that the wavelength is computed as  $\lambda = v/f$  where  $f$  is the frequency. Thus, we have  $\lambda = 3 \times 10^8 / 60 = 5,000,000$  m = 5000 km = 3106 miles.

A typical value of  $Z_c$  is 400 ohms for a single three-phase overhead line, but lower values can be found for highly bundled designs.

$$Z_c = \sqrt{\frac{z}{y}} \quad \text{with units of ohms.} \quad (1d)$$

And *cosh* and *sinh* are the hyperbolic cosine and sine functions, respectively, given by:

$$\cosh x = \frac{e^x + e^{-x}}{2}; \quad \sinh x = \frac{e^x - e^{-x}}{2}$$

Those same notes (“TerminalRelations”) show that equations (1a, 1b) may be represented using the following pi-equivalent line model

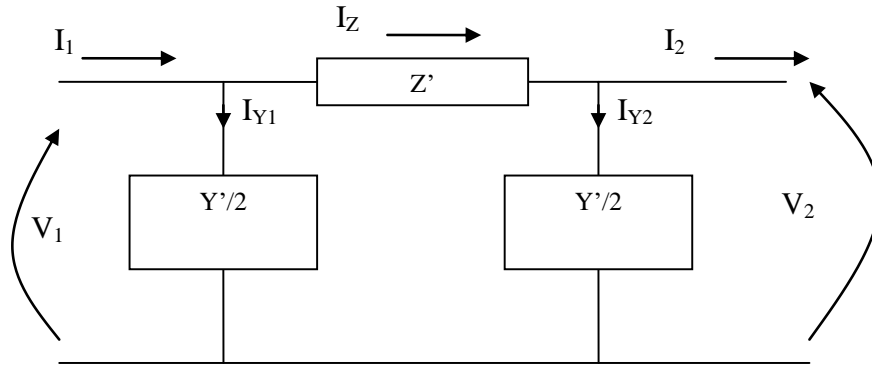


Fig. 2

where

$$Z' = Z \frac{\sinh \gamma l}{\gamma l} \quad (2a)$$

$$Y' = Y \frac{\tanh(\gamma l / 2)}{\gamma l / 2} \quad (2b)$$

and  $Z=zl$ ,  $Y=yl$ .

Two comments are necessary here:

1. Equations (2a, 2b) show that the impedance and admittance of a transmission line are not just the impedance per unit length and admittance per unit length multiplied by the line length,  $Z=zl$  and  $Y=yl$ , respectively, but they are these values corrected by the factors

$$\frac{\sinh \gamma l}{\gamma l} \quad \frac{\tanh(\gamma l / 2)}{\gamma l / 2}$$

It is of interest to note that these two factors approach 1.0 (the first from above and the second from below) as  $\gamma l$  becomes small. This fact has an important implication in that short lines (less than ~100 miles) are usually well approximated by  $Z=zl$  and  $Y=yl$ , but longer lines are not and need to be multiplied by the “correction factors” listed above. The “correction” enables the lumped parameter model to exhibit the same characteristics as the distributed parameter device.

2. We may obtain all of what we need if we have  $z$  and  $y$ . The next section will describe how to obtain them.



## 2. Obtaining per-unit length parameters

In the 9/6 and 9/8 notes at

<http://home.engineering.iastate.edu/~jdm/EE456/ee456schedule.htm>

I have derived expressions to compute per-unit length inductance and per-unit length capacitance of a transmission line given its geometry. These expressions are:

**Inductance (h/m):**  $l_a = \frac{\mu_0}{2\pi} \ln \frac{D_m}{R_b}$

$\mu_0$  is the permeability of free space, given by  $4\pi \times 10^{-7}$  Henry/meter.

- $D_m$  is the GMD between phase positions:

$$D_m \equiv (d_{ab}^{(1)} d_{ab}^{(2)} d_{ab}^{(3)})^{1/3}$$

- $R_b$  is the GMR of the bundle

$$R_b = (r' d_{12})^{1/2}, \quad \text{for 2 conductor bundle}$$

$$= (r' d_{12} d_{13})^{1/3}, \quad \text{for 3 conductor bundle}$$

$$= (r' d_{12} d_{13} d_{14})^{1/4}, \quad \text{for 4 conductor bundle}$$

$$= (r' d_{12} d_{13} d_{14} d_{15} d_{16})^{1/6}, \quad \text{for 6 conductor bundle}$$

**Capacitance (f/m):**  $\bar{c}_a = \frac{2\pi\epsilon}{\ln(D_m / R_b^c)}$

- $D_m$  is the same as above.
- $R_b^c$  is Capacitive GMR for the bundle:

$$R_b^c = (r d_{12})^{1/2}, \quad \text{for 2 conductor bundle}$$

$$= (r d_{12} d_{13})^{1/3}, \quad \text{for 3 conductor bundle}$$

$$= (r d_{12} d_{13} d_{14})^{1/4}, \quad \text{for 4 conductor bundle}$$

$$= (r d_{12} d_{13} d_{14} d_{15} d_{16})^{1/6}, \quad \text{for 6 conductor bundle}$$

$d_{ab}^{(1)}$  is distance between phases a and b under configuration (1). There are 3 configurations (1), (2), and (3) due to the common practice of transposition where phase positions are interchanged every few miles.

$d_{12}$  is the distance between conductors 1 and 2 in a bundle. Bundling is the practice of using multiple conductors in each phase.

The effects of bundling are to increase  $R_b$ . This tends to decrease inductance and therefore inductive reactance of the line.

The effects of bundling are to increase  $R_b^c$ . This tends to increase capacitance and therefore capacitive susceptance of the line.

In the above,  $r$  is the radius of a single conductor, and  $r'$  is the Geometric Mean Radius (GMR) of an individual conductor, given by

$$r' = r e^{-\frac{\mu_r}{4}} = r \times 0.7788 \quad (3)$$

It is the radius of an equivalent hollow cylindrical conductor that would have the same flux linkages as the solid conductor of radius  $r$ . (According to Ampere's Law  $\oint_{\Gamma} \underline{H} \bullet d\underline{l} = i_{EN}$ , the magnetic field is zero if the closed contour  $\Gamma$  encloses no current. Therefore, a solid conductor has flux within the conductor whereas a hollow conductor has no flux within the conductor.)

## 2.1 Inductive reactance

The per-phase inductive reactance in  $\Omega/\text{m}$  of a non-bundled transmission line is  $2\pi f l_a$ , where

$l_a = \frac{\mu_0}{2\pi} \ln \frac{D_m}{R_b} \Omega/\text{m}$ . Therefore, we can express the reactance

in  $\Omega/\text{mile}$  as

$$\begin{aligned} X_L &= 2\pi f l_a \frac{1609 \text{ meters}}{1 \text{ mile}} = 2\pi f \left( \frac{\mu_0}{2\pi} \ln \frac{D_m}{R_b} \right) \frac{1609 \text{ meters}}{1 \text{ mile}} \\ &= f \left( \mu_0 \ln \frac{D_m}{R_b} \right) \frac{1609 \text{ meters}}{1 \text{ mile}} = 2.022 \times 10^{-3} f \ln \frac{D_m}{R_b} \Omega/\text{mile} \quad (4) \end{aligned}$$

Let's expand the logarithm to get

$$X_L = \underbrace{2.022 \times 10^{-3} f \ln \frac{1}{R_b}}_{X_a} + \underbrace{2.022 \times 10^{-3} f \ln D_m}_{X_d} \Omega/\text{mile} \quad (5)$$

where  $f=60$  Hz. The first term is called the inductive reactance *at 1-foot spacing*, because it expresses equation (4) with  $D_m=1$  foot.

Note: to get  $X_a$ , you need only to know  $R_b$ , which means you need only know the conductor used and the bundling. But you do *not* need to know the geometry of the phase positions.

But what is  $X_d$ ? This is called the inductive reactance spacing factor. Note that it depends only on  $D_m$ , which is the GMD between phase positions. So you can get  $X_d$  by knowing only the distance between phases, i.e, you need not know anything about the conductor or the bundling.

## 2.2 Capacitive reactance

Similar thinking for capacitive reactance leads to

$$X_C = \underbrace{\frac{1}{f} \times 1.779 \times 10^6 \ln \left( \frac{1}{R_b^c} \right)}_{X'_a} + \underbrace{\frac{1}{f} \times 1.779 \times 10^6 \ln(D_m)}_{X'_d} \Omega - \text{mile}$$

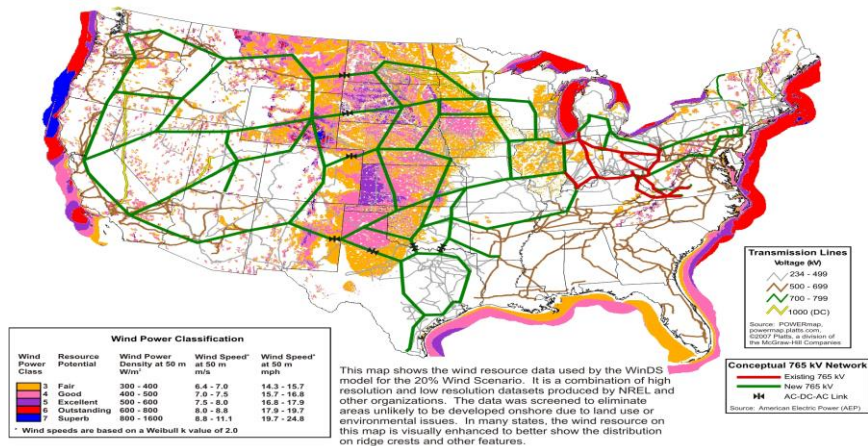
$X'_a$  is the capacitive reactance at 1 foot spacing, and  $X'_d$  is the capacitive reactance spacing factor. Note the units are

ohms-mile, instead of ohms/mile, so that when we invert, we will get mhos/mile, as desired.

### 3. Example

A circular mil is a unit of area, equal to the area of a circle with a diameter 1mil (1 mil=0.001in=0.0254 mm). It corresponds to approximately  $5.067 \times 10^{-4} \text{ mm}^2$ . ... 1000 circular mil equals  $0.5067 \text{ mm}^2$ . The area of a circle of a circle of 1 mil is  $\pi r^2 = \pi(d/2)^2$ , or  $\pi(10^{-3}\text{in}/2)^2 = 7.854 \times 10^{-7} \text{ in}^2$ .

Let's compute the  $X_L$  and  $X_C$  for a 765 kV AC line, single circuit, with a 6 conductor bundle per phase, using conductor type Tern (795 kcmil). AEP considered a similar design a few years ago when they proposed a 765kV transmission overlay for the nation, shown below.



The bundles have 2.5' (30") diameter, and the phases are separated by 45', as shown in Fig. 3. Assume the line is lossless.

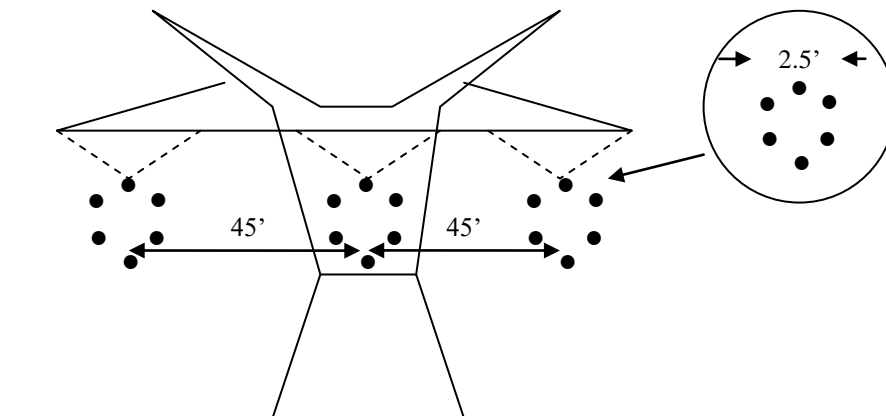


Fig. 3



We will use tables from [1] (available in pdf [2]), which I have copied out and placed on the website. Noting the below table (obtained from [3] and placed on the website), this example focuses on line geometry AEP 3.

TABLE 2 LINE GEOMETRIES

Company/Country	Nominal Voltage (kV)	No. of Sub-conductors	Conductor Diameter (cm)	Phase Spacing (m)	Min. Conductor Heights* (m)
Hydro-Québec 1	735	4	3.50	15.3	15.3
Hydro-Québec 2	735	4	3.56	12.8	14.1
AEP 1	765	4	2.96	13.7	12.2
AEP 2	765	4	3.52	13.7	12.2/13.7
AEP 3	765	6	2.70	13.7	13.7
NYPA	765	4	3.52	15.2	15.5
Eskom	765	6	2.86	15.8	15.0
FURNAS	765	4	3.20	14.3	13
EDELCA 1 & 2	765	4	3.33	15.0	14.7
EDELCA 3	765	4	3.33	13.2	13.7
KEPCO	765	6	3.042	See Note 1	19/28
POWERGRID	765	4	3.50	15.4	15
RUSSIA 1	750	5	2.24	17.5	12
RUSSIA 2	750	4	2.91	19	12
RUSSIA 3	1150	8	2.75	21.5-25	17.5
TEPCO	1000	8	3.42/3.84**	See Note 1	25/35
* Minimum heights in areas frequented by people including agricultural areas.					
** Larger conductor used in populated areas; smaller conductor used in mountainous areas.					
1. Double-circuit low reactance line					

The tables show data for 24” and 36” 6-conductor bundles, but not 30”, and so we must interpolate.

Get per-unit length inductive reactance:

From Table 3.3.1, we find

INDUCTIVE REACTANCE ( $X_a$ ) OF BUNDLED CONDUCTORS AT 60 HZ IN OHMS PER MILE FOR ONE-FOOT SPACING															
Code	(kcmil) (sq mm)		Strand	5-Cond Bundle Diam			8-Cond Bundle Diam			12-Cond Bundle Diam			16-Cond Bundle Diam		
	Al	Tot		24	36	54	27	40	60	33	50	75	40	60	90
Aluminum-Conductor-Steel-Reinforced (ACSR)															
—	2776	1521	84/19	0.019	-0.022	-0.063	-0.003	-0.045	-0.088	-0.035	-0.079	-0.124	-0.057	-0.105	-0.151
Joree	2515	1344	76/19	0.020	-0.021	-0.062	-0.002	-0.044	-0.087	-0.032	-0.079	-0.124	-0.058	-0.104	-0.150
Thrasher	2312	1235	76/19	0.021	-0.020	-0.061	-0.001	-0.043	-0.086	-0.032	-0.078	-0.123	-0.058	-0.104	-0.150
Kiwi	2167	1146	72/7	0.022	-0.019	-0.060	-0.001	-0.042	-0.085	-0.032	-0.078	-0.123	-0.057	-0.104	-0.150
Bluebird	2156	1181	84/19	0.021	-0.020	-0.061	-0.001	-0.043	-0.086	-0.032	-0.078	-0.123	-0.058	-0.104	-0.150
Chukar	1781	976	84/19	0.023	-0.018	-0.059	0.000	-0.041	-0.084	-0.031	-0.077	-0.122	-0.057	-0.103	-0.149
Falcon	1590	908	54/19	0.024	-0.017	-0.058	0.001	-0.041	-0.084	-0.031	-0.077	-0.122	-0.057	-0.103	-0.149
Plover	1431	817	54/19	0.025	-0.016	-0.057	0.002	-0.040	-0.083	-0.030	-0.076	-0.121	-0.056	-0.102	-0.149
Bobolink	1431	775	45/7	0.026	-0.015	-0.056	0.002	-0.039	-0.083	-0.030	-0.076	-0.121	-0.056	-0.102	-0.148
Pheasant	1272	726	54/19	0.026	-0.015	-0.056	0.002	-0.039	-0.082	-0.030	-0.076	-0.121	-0.056	-0.102	-0.148
Bittern	1272	689	45/7	0.027	-0.014	-0.055	0.003	-0.039	-0.082	-0.029	-0.075	-0.120	-0.056	-0.102	-0.148
Finch	1114	636	54/19	0.027	-0.014	-0.055	0.003	-0.038	-0.081	-0.029	-0.075	-0.120	-0.056	-0.102	-0.148
Bluejay	1113	603	45/7	0.028	-0.013	-0.054	0.004	-0.038	-0.081	-0.028	-0.075	-0.120	-0.055	-0.101	-0.147
Ortolan	1034	560	45/7	0.029	-0.012	-0.053	0.005	-0.037	-0.080	-0.028	-0.074	-0.119	-0.055	-0.101	-0.147
Cardinal	954	546	54/7	0.029	-0.012	-0.053	0.005	-0.037	-0.080	-0.028	-0.074	-0.119	-0.055	-0.101	-0.147
Rail	954	517	45/7	0.030	-0.011	-0.052	0.005	-0.036	-0.079	-0.028	-0.074	-0.119	-0.054	-0.101	-0.147
Drake	795	469	26/7	0.030	-0.011	-0.052	0.006	-0.036	-0.079	-0.027	-0.074	-0.119	-0.054	-0.100	-0.146
Condor	796	456	54/7	0.031	-0.010	-0.051	0.006	-0.036	-0.079	-0.027	-0.073	-0.118	-0.054	-0.100	-0.145
Cuckoo	795	455	24/7	0.031	-0.010	-0.051	0.006	-0.036	-0.079	-0.027	-0.073	-0.118	-0.054	-0.100	-0.146
Tern	795	431	45/7	0.031	-0.010	-0.051	0.007	-0.035	-0.078	-0.027	-0.073	-0.118	-0.054	-0.100	-0.146

24" bundle: 0.031

36" bundle: -0.010

30" bundle: interpolation results in  $X_a=0.0105$ .

From Table 3.3.12, we find

ft	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
45	0.4619	0.4622	0.4624	0.4627	0.4630	0.4632	0.4635	0.4638	0.4640	0.4643
46	0.4646	0.4648	0.4651	0.4654	0.4656	0.4659	0.4661	0.4664	0.4667	0.4669
47	0.4672	0.4674	0.4677	0.4680	0.4682	0.4685	0.4687	0.4690	0.4692	0.4695
48	0.4697	0.4700	0.4702	0.4705	0.4707	0.4710	0.4712	0.4715	0.4717	0.4720
49	0.4722	0.4725	0.4727	0.4730	0.4732	0.4735	0.4737	0.4740	0.4742	0.4744

45' phase spacing:  $X_d=0.4619$

And so  $X_L=X_a+X_d=0.0105+0.4619=0.4724$  ohms/mile.

Now get per-unit length capacitive reactance.

From Table 3.3.2, we find

**Table 3.3.2 (Cont.)**  
**CAPACITIVE REACTANCE ( $X'_c$ ) OF BUNDLED CONDUCTORS AT 60 HZ IN MEGOHM-MILES FOR ONE-FOOT SPACING**

Code	(kcmil) (sq mm)		Strand	6-Cond Bundle Diam			8-Cond Bundle Diam			12-Cond Bundle Diam			16-Cond Bundle Diam		
	Al	Tot		24	36	54	27	40	60	33	50	75	40	60	90
Aluminum-Conductor-Steel-Reinforced (ACSR)															
Jorec	2776	1521	84/19	0.0034	-0.0066	-0.0166	-0.0016	-0.0117	-0.0223	-0.0086	-0.0199	-0.0309	-0.0147	-0.0260	-0.0372
	2515	1344	76/19	0.0037	-0.0063	-0.0163	-0.0013	-0.0115	-0.0220	-0.0085	-0.0198	-0.0308	-0.0146	-0.0259	-0.0371
	2312	1235	76/19	0.0039	-0.0061	-0.0161	-0.0012	-0.0114	-0.0219	-0.0084	-0.0197	-0.0307	-0.0145	-0.0258	-0.0371
	2167	1146	72/7	0.0041	-0.0059	-0.0159	-0.0010	-0.0112	-0.0217	-0.0083	-0.0196	-0.0306	-0.0145	-0.0257	-0.0370
Bluebird	2156	1181	84/19	0.0040	-0.0060	-0.0160	-0.0011	-0.0113	-0.0218	-0.0083	-0.0196	-0.0306	-0.0145	-0.0257	-0.0370
Chukar	1781	976	84/19	0.0045	-0.0055	-0.0155	-0.0007	-0.0109	-0.0214	-0.0081	-0.0194	-0.0304	-0.0143	-0.0256	-0.0368
Falcon	1590	908	54/19	0.0047	-0.0053	-0.0153	-0.0006	-0.0108	-0.0213	-0.0080	-0.0193	-0.0303	-0.0142	-0.0255	-0.0368
Plover	1431	817	54/19	0.0050	-0.0051	-0.0151	-0.0004	-0.0106	-0.0211	-0.0079	-0.0192	-0.0302	-0.0141	-0.0254	-0.0367
Bobolink	1431	775	45/7	0.0051	-0.0049	-0.0149	-0.0003	-0.0105	-0.0210	-0.0078	-0.0191	-0.0301	-0.0141	-0.0254	-0.0366
Pheasant	1272	726	54/19	0.0052	-0.0048	-0.0148	-0.0002	-0.0104	-0.0209	-0.0077	-0.0190	-0.0300	-0.0140	-0.0253	-0.0366
Bittern	1272	689	45/7	0.0054	-0.0046	-0.0146	-0.0001	-0.0103	-0.0208	-0.0077	-0.0190	-0.0300	-0.0140	-0.0252	-0.0365
Finch	1114	636	54/19	0.0056	-0.0044	-0.0144	0.0001	-0.0101	-0.0206	-0.0076	-0.0189	-0.0299	-0.0139	-0.0252	-0.0364
Bluejay	1113	603	45/7	0.0057	-0.0043	-0.0143	0.0002	-0.0100	-0.0205	-0.0075	-0.0188	-0.0298	-0.0139	-0.0251	-0.0364
Ortolan	1034	580	45/7	0.0059	-0.0041	-0.0141	0.0003	-0.0099	-0.0204	-0.0074	-0.0187	-0.0297	-0.0138	-0.0251	-0.0363
Cardinal	954	546	54/7	0.0060	-0.0040	-0.0141	0.0004	-0.0098	-0.0203	-0.0074	-0.0187	-0.0297	-0.0138	-0.0250	-0.0363
Rail	954	517	45/7	0.0061	-0.0039	-0.0139	0.0004	-0.0097	-0.0203	-0.0073	-0.0186	-0.0296	-0.0137	-0.0250	-0.0362
Drake	795	469	26/7	0.0063	-0.0037	-0.0137	0.0006	-0.0096	-0.0201	-0.0072	-0.0185	-0.0295	-0.0136	-0.0249	-0.0362
Condor	796	456	54/7	0.0064	-0.0036	-0.0136	0.0007	-0.0095	-0.0200	-0.0072	-0.0184	-0.0295	-0.0136	-0.0249	-0.0361
Cuckoo	795	455	24/7	0.0064	-0.0036	-0.0136	0.0007	-0.0095	-0.0200	-0.0072	-0.0184	-0.0295	-0.0136	-0.0249	-0.0361
Tern	795	431	45/7	0.0065	-0.0035	-0.0135	0.0008	-0.0094	-0.0199	-0.0071	-0.0184	-0.0294	-0.0136	-0.0248	-0.0361

24" bundle: 0.065

36" bundle: -0.0036

30" bundle: interpolation results in  $X'_a=0.0307$ .

From Table 3.3.13, we find

Table 3.3.13 SHUNT CAPACITIVE REACTANCE SPACING FACTOR, $X'_d$ , AT 60 HZ (MEGOHM-MILES)										
ft	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
45	0.1128	0.1128	0.1129	0.1130	0.1130	0.1131	0.1132	0.1132	0.1133	0.1134
46	0.1134	0.1135	0.1136	0.1136	0.1137	0.1138	0.1138	0.1139	0.1139	0.1140
47	0.1141	0.1141	0.1142	0.1143	0.1143	0.1144	0.1144	0.1145	0.1146	0.1146
48	0.1147	0.1148	0.1148	0.1149	0.1149	0.1150	0.1151	0.1151	0.1152	0.1152
49	0.1153	0.1154	0.1154	0.1155	0.1155	0.1156	0.1157	0.1157	0.1158	0.1158

45' phase spacing:  $X'_d=0.1128$

And so  $X_C=X'_a+X'_d=0.0307+0.1128=0.1435$  Mohms-mile.  
 Note the units of  $X_C$  are ohms-mile $\times 10^6$  [so that  $B_C=1/X_C$  has units of  $1/(\text{ohms-mile}\times 10^6)=\text{Mhos}\times 10^{-6}/\text{mile}$ ].

So  $z=jX_L=j0.4724$  Ohms/mile, and this is for the 6 bdl, 765 kV circuit.

And  $y=1/-jX_C=1/-j(0.1435 \times 10^6)=j6.9686 \times 10^{-6}$  Mhos/mile

Now compute the propagation constant,  $\gamma$ ,

$$\gamma = \sqrt{zy} = \sqrt{j0.4724 \times j6.9686 \times 10^{-6}}$$

$$= \sqrt{-3.292 \times 10^{-6}} = j0.0018 / \text{mile}$$

Recalling (2a, 2b)

$$Z' = Z \frac{\sinh \gamma l}{\gamma l} \quad (2a)$$

$$Y' = Y \frac{\tanh(\gamma l / 2)}{\gamma l / 2} \quad (2b)$$

The propagation constant  $\gamma$  of an electromagnetic wave is a measure of the change undergone by the amplitude of the wave as it propagates in a given direction.  $\gamma$  is in general complex, so that  $\gamma = \alpha + j\beta$ . For a lossless transmission line,  $\gamma = j\beta$ .

$\beta$ , the phase constant, determines the wavelength, given by  $\lambda = 2\pi/\beta$ . For the example, we obtain  $\lambda = 2\pi/0.0018 = 3463$  miles which means it requires 3463 miles to complete  $2\pi$  radians of the wave.

Let's do two calculations:

- The circuit is 100 miles in length. Then  $l=100$ , and
 
$$Z = j.4724 \text{ ohms} / \text{mile} * 100 \text{ miles} = j47.24 \text{ ohms}$$

$$Y = j6.986 \times 10^{-6} \text{ mhos} / \text{mile} * 100 \text{ miles} = j0.0006986 \text{ mhos}$$

$$\gamma l = \frac{j0.0018}{\text{mile}} (100 \text{ miles}) = j0.18$$

Convert  $Z$  and  $Y$  to per-unit,  $V_b=765\text{kV}$ ,  $S_b=100$  MVA

$$Z_b = (765 \times 10^3)^2 / 100 \times 10^6 = 5852.3 \text{ ohms},$$

$$Y_b = 1/5852.3 = 0.00017087 \text{ mhos}$$

$$Z_{pu} = j47.24/5852.3 = j0.0081 \text{ pu},$$

$$Y_{pu} = j0.0006986/.00017087 = j4.0885 \text{ pu}$$

$$Z' = Z \frac{\sinh \gamma l}{\gamma l} = j0.0081 \frac{\sinh(j.18)}{j.18} = j0.0081 \frac{j.179}{j.18} = j0.00806$$

$$Y' = Y \frac{\tanh(\gamma l / 2)}{\gamma l / 2} = j4.0885 \frac{\tanh(j.18 / 2)}{j.18 / 2} = j4.0885 \frac{j0.0902}{j.09} = j4.0976$$

- The circuit is 500 miles in length. Then  $l=500$ , and  
 $Z = j.4724 \text{ ohms} / \text{mile} * 500 \text{ miles} = j236.2 \text{ ohms}$
- $Y = j6.986 \times 10^{-6} \text{ mhos} / \text{mile} * 500 \text{ miles} = j0.0035 \text{ mhos}$

$$\gamma l = \frac{j0.0018}{\text{mile}} (500 \text{ miles}) = j0.90$$

Convert  $Z$  and  $Y$  to per-unit,  $V_b=765\text{kV}$ ,  $S_b=100 \text{ MVA}$

$$Z_{pu} = j236.2 / 5852.3 = j0.0404 \text{ pu},$$

$$Y_{pu} = j0.0035 / .00017087 = j20.4834 \text{ pu}$$

$$Z' = Z \frac{\sinh \gamma l}{\gamma l} = j.0404 \frac{\sinh(j.90)}{j.90} = j.0404 \frac{j.7833}{j.90} = j.0352$$

$$Y' = Y \frac{\tanh(\gamma l / 2)}{\gamma l / 2} = j20.4834 \frac{\tanh(j.90 / 2)}{j.90 / 2} = j20.4834 \frac{j0.4831}{j.45} = j21.99$$

It is of interest to calculate the surge impedance for this circuit. From eq. (1d), we have

$$Z_C = \sqrt{\frac{z}{y}} = \sqrt{\frac{j.4724}{j6.9686 \times 10^{-6}}} = 260.3647 \text{ ohms}$$

A line terminated in  $Z_C$  has a very special character with respect to reactive power: the amount of reactive power consumed by the series  $X$  is exactly compensated by the reactive power supplied by the shunt  $Y$ , for every inch of the line. In addition, such a line appears to the source as an infinitely long line; it produces no reflections.

Then the surge impedance loading is given by

$$P_{SIL} = \frac{V_{LL}^2}{Z_C} = \frac{(765 \times 10^3)^2}{260.3647} = 2.2477 \times 10^9$$

The SIL for this circuit is 2247 MW. We estimate line loadability from the Fig. 4 St. Clair curves as a function of line length (we further discuss these curves later).

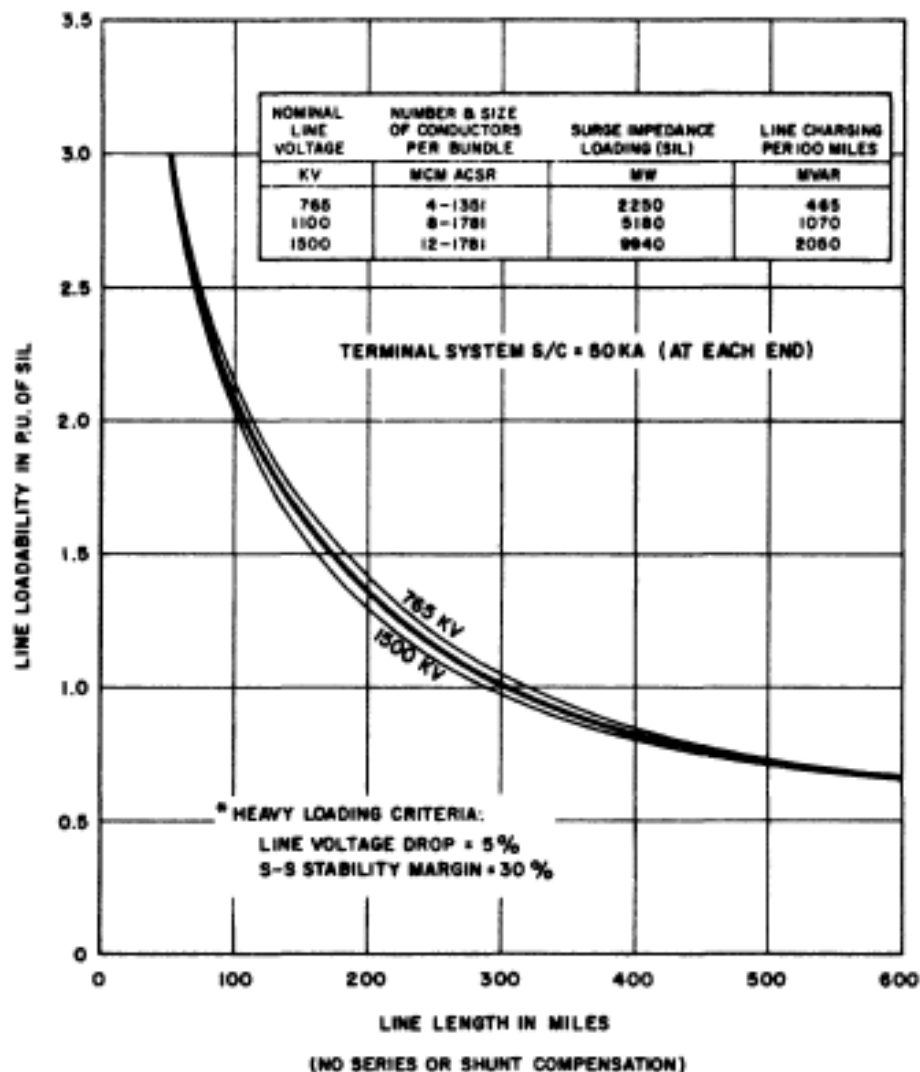


Fig. 4

100 mile long line:  $P_{\max} = 2.1(2247) = 4719$  MW.

500 mile long line:  $P_{\max} = 0.75(2247) = 1685$  MW.

#### **4. Conductor ampacity**

A conductor expands when heated, and this expansion causes it to sag. Conductor surface temperatures are a function of the following:

- a) Conductor material properties
- b) Conductor diameter
- c) Conductor surface conditions
- d) Ambient weather conditions
- e) Conductor electrical current

IEEE Standard 738-2006 (IEEE Standard for Calculating Current–Temperature Relationship of Bare Overhead Conductors) [4] provides an analytic model for computing conductor temperature based on the above influences.

In addition, this same model is used to compute the conductor current necessary to cause a “maximum allowable conductor temperature” under “assumed conditions.”

- **Maximum allowable conductor temperature:** This temperature is normally selected so as to limit either conductor loss of strength due to the annealing of aluminum or to maintain adequate ground clearance, as required by the National Electric Safety Code. This temperature varies widely according to conductor type and engineering practice and judgment [4], with 100 °C being not uncommon.

- Assumed conditions: It is good practice to select “conservative” weather conditions such as 0.6 m/s to 1.2 m/s wind speed (2ft/sec-4ft/sec), 30 °C to 45 °C (86°F-113°F) for summer conditions.

Given this information, the corresponding conductor current (I) that produced the maximum allowable conductor temperature under these weather conditions can be found from the steady-state heat balance equation [4].

For example, the Tern conductor used in the 6 bundle 765kV line (see example above) is computed to have an ampacity of about 860 amperes at 75 °C conductor temperature, 25 °C ambient temperature, and 2 ft/sec wind speed. At 6 conductors per phase, this allows for  $6 \times 860 = 5160$  amperes, which would correspond to a power transfer of  $\sqrt{3} * 765000 * 5160 = 6837$  MVA.

Recall the SIL for this line was 2247 MW. Figure 4 indicates the short-line power handling capability of this circuit should be about  $3(2247) = 6741$  MW. (Note that Fig. 4 shows the power limit does not exceed this value.)

➔ Short-line limitations are thermal-constrained.

When considering relatively long lines, you will not need to be too concerned about ampacity. Limitations of an amount equal to the SIL or lower will be more appropriate to use for these long lines.



## 5.0 St. Clair Curves

Figure 4 is a well-known curve that should be considered as a planning guide and not an exact relationship. But as a planning guide, it is very useful. You should have some understanding of how this curve is developed. Refer to [5], a predecessor paper [6], a summary [7], and an extension (for voltage instability) in [8] for more details.

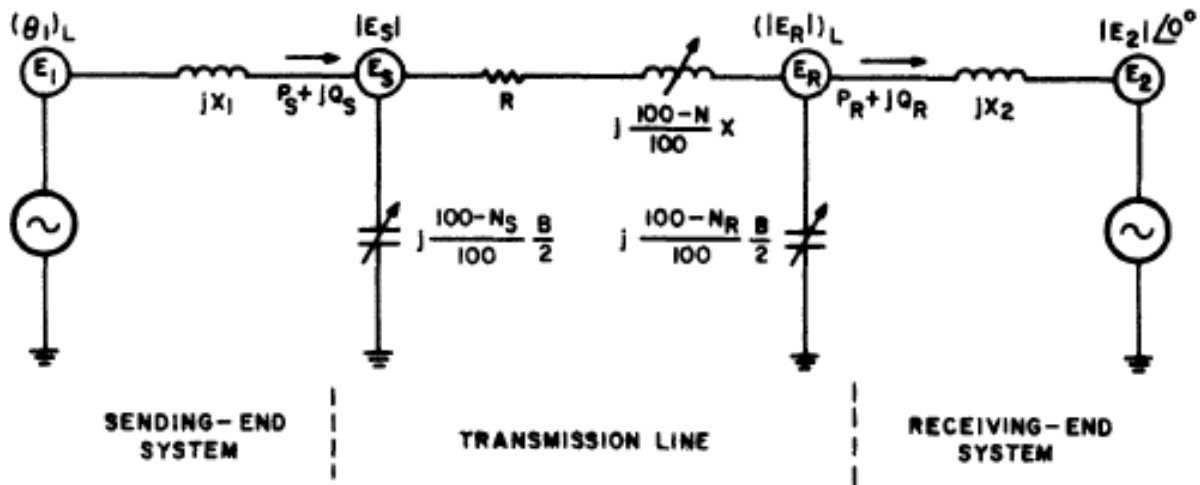
This curve represents three different types of limits:

- Short-line limitation at approximately 3 times SIL
- Medium-line limitation corresponding to a limit of a 5% voltage drop across the line;
- A long-line limitation corresponding to a limit of a 44 degree angular separation across the line.

This curve was developed based on the following circuit in Fig. 5.

Given:  $R, X, B, X_1, X_2, \theta_1, |E_2|, |E_S|$   
Find:  $|E_1|, \theta_s, |E_R|, \theta_R$

Write 2 KCL equations at the nodes corresponding to  $E_S$  and  $E_R$ ; then separate these into real & imaginary parts, giving 4 equations to find 4 unknowns.



**Figure 3.** Mathematical model developed for line loadability study

- $R$  - positive-sequence resistance\*
- $X$  - positive-sequence inductive reactance\*
- $B$  - positive-sequence capacitive susceptance\*

\* corrected for long-line effect

Fig. 5

This circuit was analyzed using the following algorithm, Fig. 6. Observe the presence of the voltage source  $E_2$ , which is used to represent reactive resources associated with the receiving end of the transmission line. The reactances  $X_1$  and  $X_2$  represent the transmission system at the sending and receiving ends, respectively.

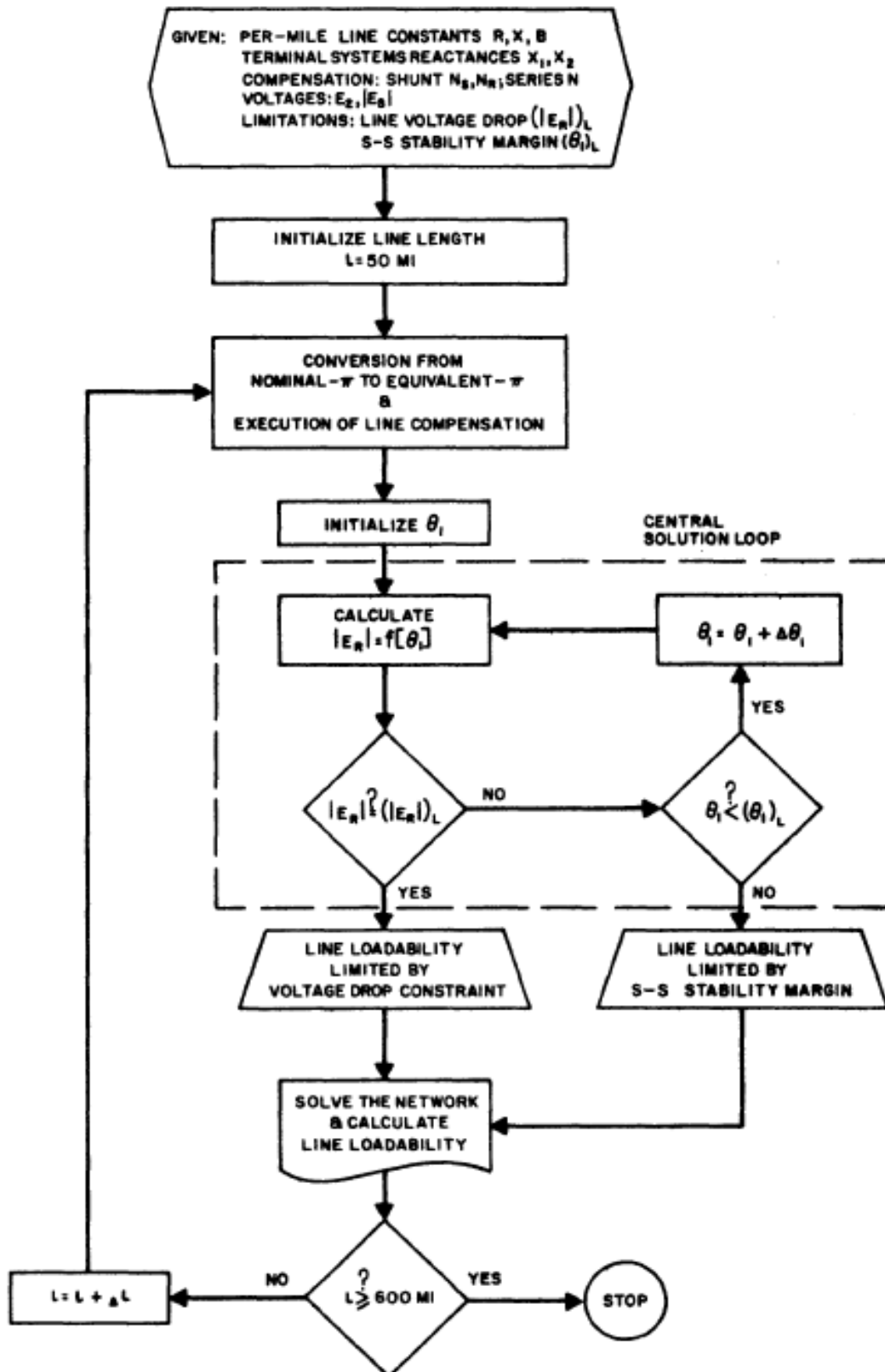


Fig. 6

The key calculation performed in the algorithm is represented by block having the statement

CALCULATE

$$|E_R|=f(\theta_1)$$

Referring to the circuit diagram, this problem is posed as:

Given:  $R, X, B, X_1, X_2, \theta_1, |E_2|, |E_S|$

Find:  $|E_1|, \theta_s, |E_R|, \theta_R$

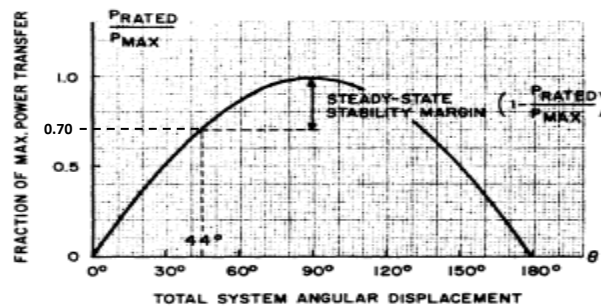
Although the paper does not say much about how it makes this calculation, one can write two KCL equations at the two nodes corresponding to  $E_S$  and  $E_R$ , and then separate these into real and imaginary parts, giving 4 equations to find 4 unknowns (note that the angle of  $E_2$  is assumed to be the reference angle and thus is 0 degrees).

The result of this analysis for a particular line design (bundle and phase geometry) is shown in Fig. 7, where we observe two curves corresponding to

- Constant steady-state stability margin curve of 30% (angle is  $\theta_1$ , which is from node  $E_1$  to node  $E_2$ ).

This value is computed based on

$$\% \text{Stability Margin} = \frac{P_{\max} - P_{\text{rated}}}{P_{\max}} \times 100\%$$



Here,  $P_{\max}$  is the ampacity of the line, and  $P_{\text{rated}}$  is the allowable flow on the line.

- Constant line voltage drop curve of 5%, given by

$$\% \text{ Voltage Drop} = \frac{E_s - E_r}{E_s} \times 100\%$$

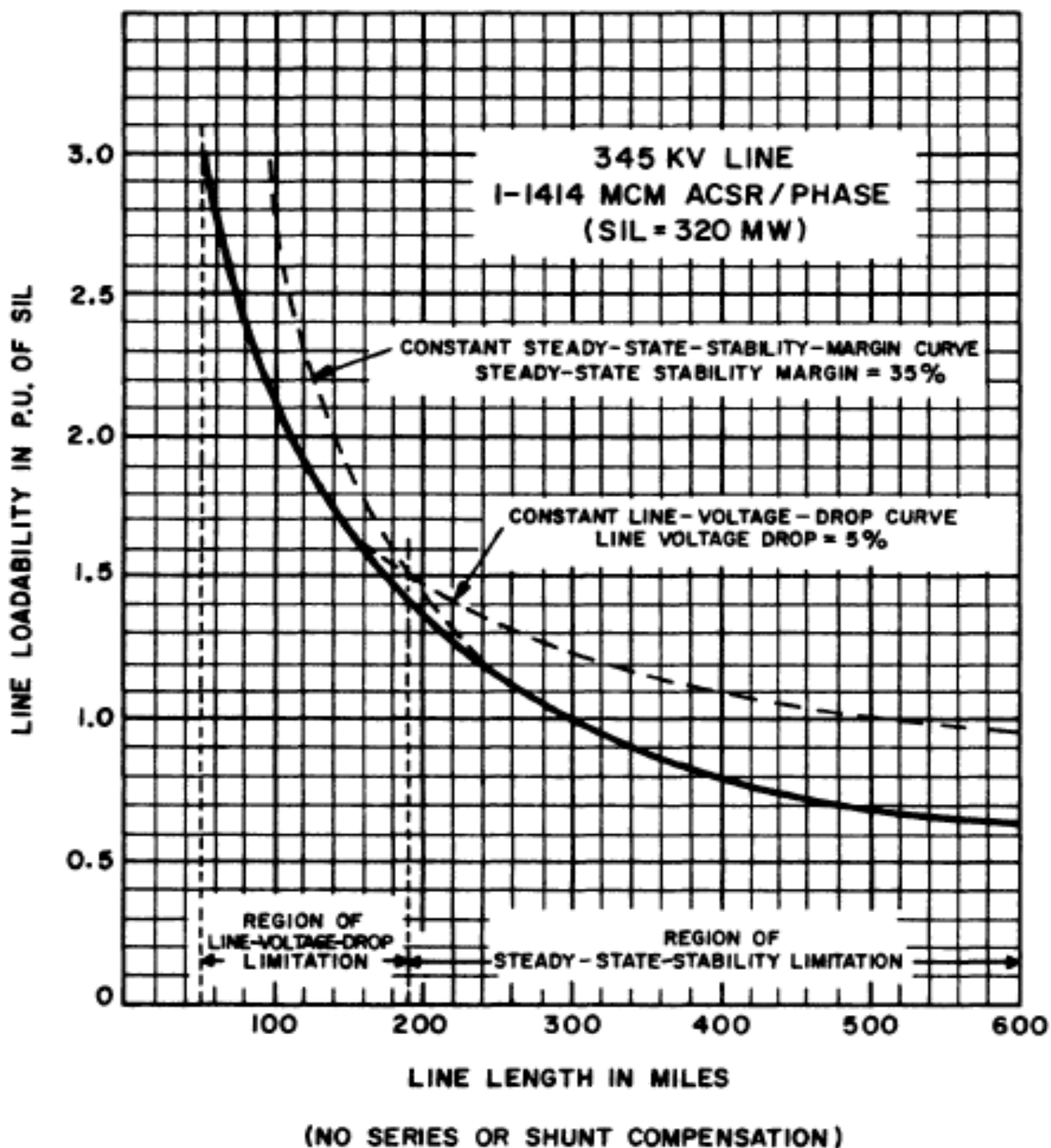


Fig. 7

In Fig. 7, the dark solid curve is the composite of the two limitations associated with steady-state stability and voltage drop. The 3.0 pu SIL value which limits the curve at short distances is associated with the conductor's thermal limit.

The paper being discussed [5], in addition to 345 kV, also applies its approach to higher voltage transmission, 765 kV, 1100 kV, and 1500 kV (Unfortunately, for some reason, 500 kV was not included). For these various transmission voltages, it presents a table of data that can be used in the circuit of Fig. 5 and the algorithm of Fig. 6. This table is copied out below.

NOMINAL VOLTAGE CLASS (kV)	SYSTEM STRENGTH AT EACH TERMINAL*		LINE CHARACTERISTICS**		
	MVA <sub>3φ</sub>	$\% X = \frac{100}{MVA_{3\phi}} \cdot 100\%$	Z (%/mi)	Y (%/mi)	SIL (MW)
345	30,000	.333	.00571 + j.06432	j.6604	320
765	66,000	.151	.00033 + j.00918	j4.659	2250
1100 <sup>(6)</sup>	95,000	.105	.00007 + j.00398	j10.69	5180
1500 <sup>(6)</sup>	130,000	.077	.00003 + j.00207	j20.51	9940

\* SYSTEM STRENGTH CORRESPONDING TO 50KA FAULT DUTY

\*\* POSITIVE-SEQUENCE CHARACTERISTICS (ON 100 MVA BASE)

The “system strength at each terminal”<sup>1</sup> is quantified by the fault duty at that terminal, assumed in both cases to be

<sup>1</sup> The fault duty or short circuit current at a bus provides an indication of the network's voltage “stiffness” or “strength” at that bus. The higher a bus's short circuit current, the lower the impedance between that bus and current sources (generators), the less the variation in voltage magnitude will occur for a given change in network conditions.

50 kA. Using this, we can get the fault duty in MVA according to

$$MVA_{3\phi} = \sqrt{3} \times V_{LL,nom} \times 50E3$$

Then the corresponding reactance may be computed by

$$X_{pu} = \frac{V_{pu}^2}{MVA_{pu}}$$

This pu reactance is computed at each terminal and used to represent the sending and receiving end impedances  $X_1$  and  $X_2$  respectively (see Fig. 5).

**This can be shown as follows:**

$$S_{3\phi} = 3V_{LN}^2/X.$$

Writing all S, V, and X quantities as products of their pu values and their base quantities, we get

$$S_{3\phi,base} S_{pu} = 3[(V_{pu} V_{LN,base})^2 / (X_{pu} X_{base})]$$

Rearranging,

$$S_{3\phi,base} S_{pu} = [3V_{LN,base}^2 / X_{base}] [(V_{pu})^2 / X_{pu}]$$

And we see that

$$S_{3\phi,base} = 3V_{LN,base}^2 / X_{base} \text{ and}$$

$$S_{pu} = (V_{pu})^2 / X_{pu}$$

$$\rightarrow X_{pu} = V_{pu}^2 / S_{pu}.$$

We will assume that  $V_{pu} = 1$ , and with a 100 MVA base, the last equation results in

$$X_{pu} = \frac{1}{MVA_{3\phi} / 100} = \frac{100}{MVA_{3\phi}}$$

For example, let's consider the 765 kV circuit, then we obtain

$$\begin{aligned} MVA_{3\phi} &= \sqrt{3} \times V_{LL,nom} \times 50000 \\ &= \sqrt{3} \times 765000 \times 50000 = 6.6251E10 \quad \text{volt-amperes} \end{aligned}$$

which is 66,251 MVA.

Observe the table above gives 66,000 MVA.

Then,  $X_{pu}=100/66,000=0.00151pu$   
which is 0.151%, as given in the table.

The table also provides line impedance and susceptance, which can be useful for rough calculations. Note that the values are given in % per mile, which are 100 times the values given in pu per mile.

Finally, the table provides the surge impedance loading (SIL) of the transmission lines at the four different voltage levels, as

320, 2250, 5180, and 9940 MW for  
345, 765, 1100, and 1500 kV,  
respectively.

Recall what determines SIL:

$$P_{SIL} = \frac{V_{LL}^2}{Z_C} \quad Z_C = \sqrt{\frac{z}{y}} = \sqrt{X_L X_C}$$

$$X_L = \underbrace{2.022 \times 10^{-3} f \ln \frac{1}{R_b}}_{X_a} + \underbrace{2.022 \times 10^{-3} f \ln D_m}_{X_d} \quad \Omega/\text{mile}$$

$$X_C = \underbrace{\frac{1}{f} \times 1.779 \times 10^6 \ln \left( \frac{1}{R_b^c} \right)}_{X'_a} + \underbrace{\frac{1}{f} \times 1.779 \times 10^6 \ln(D_m)}_{X'_d} \quad \Omega - \text{mile}$$



$D_m$  is the GMD between phase positions:

$$D_m \equiv \left( d_{ab}^{(1)} d_{ab}^{(2)} d_{ab}^{(3)} \right)^{1/3}$$

$R_b$  is the GMR of the bundle

$$\begin{aligned} R_b &= (r' d_{12})^{1/2}, & \text{for 2 conductor bundle} \\ &= (r' d_{12} d_{13})^{1/3}, & \text{for 3 conductor bundle} \\ &= (r' d_{12} d_{13} d_{14})^{1/4}, & \text{for 4 conductor bundle} \\ &= (r' d_{12} d_{13} d_{14} d_{15} d_{16})^{1/6}, & \text{for 6 conductor bundle} \end{aligned}$$

$$r' = r e^{-\frac{\mu_r}{4}}$$

$R_b^c$  is Capacitive GMR for the bundle:

$$\begin{aligned} R_b^c &= (r d_{12})^{1/2}, & \text{for 2 conductor bundle} \\ &= (r d_{12} d_{13})^{1/3}, & \text{for 3 conductor bundle} \\ &= (r d_{12} d_{13} d_{14})^{1/4}, & \text{for 4 conductor bundle} \\ &= (r d_{12} d_{13} d_{14} d_{15} d_{16})^{1/6}, & \text{for 6 conductor bundle} \end{aligned}$$

So in conclusion, we observe that SIL is determined by

- Phase positions (which determines  $D_m$ )
- Choice of conductor (which determines  $r$  and  $r'$  and influences  $R_b$  and  $R_b^c$ )
- Bundling (which influences  $R_b$  and  $R_b^c$ ).

We refer to data which determines SIL as “line constants.” (Although SIL is also influenced by voltage level, the line loadability limit,  $P_{\text{rated}}/P_{\text{SIL}}$ , is not.)

Reference [5] makes a startling claim (*italics added*):

“Unlike the 345-kV or 765-kV line parameters, UHV line data is still tentative because both the choice of voltage level and optimum line design are not finalized. This uncertainty about the line constants, however, is not very critical in determining the line loadability -- expressed in per-unit of rated SIL – especially at UHV levels. The reason lies in the fact that *for a lossless line*, it can be shown that the line loadability -- or the receiving-end power -- in terms of SIL of that line,  $S_R/SIL$ , is not dependent on the line constants, but rather is a function of the line length and its terminal voltages. This concept is discussed further in the Appendix.”

Translation:  
1100 and 1500 kV transmission have never been built and so we are really just guessing in regards to its line constants...

...but it does not matter, because  $P_{rated}/P_{SIL}$  is almost independent of line constants but rather depends on just the line length and terminal voltages.

The paper’s appendix derives this result for a lossless line:

$$\frac{P_{rated}}{P_{SIL}} = j \frac{\left( \frac{E_S}{E_R} \right)^* - \cos \beta L}{\sin \beta L} |E_R|^2$$

where  $\beta = \omega/v$  and  $\omega$  is  $2\pi f$  ( $f=60\text{Hz}$ ), and  $v$  is approximately the speed of light ( $3E8\text{m/sec}$ ).

The paper justifies the “lossless line” requirement:

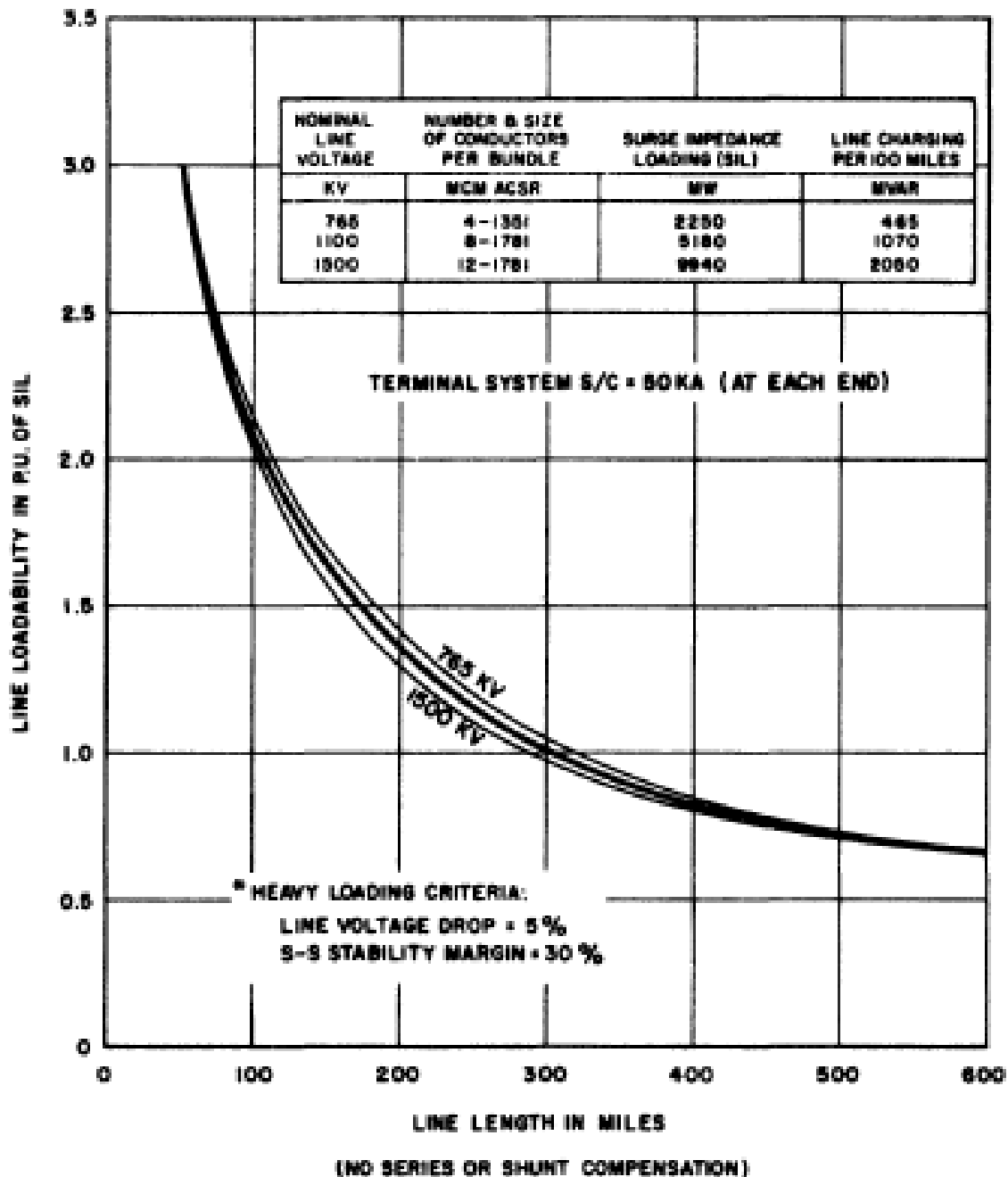
“Since the resistance of the EHV/UHV lines is much smaller than their 60-Hz reactance, such lines closely approximate a lossless line from the standpoint of loadability analysis. Therefore, the loadabilities in per-unit of SIL of these lines are practically independent of their respective line constants and, as a result, of their corresponding voltage classes.”

The paper develops the St. Clair curves for a 765 kV, 1100 kV, and a 1500 kV transmission line, and I have replicated it in Fig. 8 below. Observe that the three curves are almost identical. The paper further states (*italics added*):

“It is reassuring to know that one single curve can be applied to all voltage classes in the EHV/UHV range. Obviously, a general transmission loading curve will not cover the

complete range of possible applications; *nonetheless, it can provide a reasonable basis for any preliminary estimates of the amount of power that can be transferred over a well-designed transmission system.*"

**TRANSMISSION LINE LOADABILITY \*  
IN TERMS OF  
SURGE IMPEDANCE LOADING (SIL)**



Or... it can provide a reasonable basis for a preliminary estimate of the transmission system voltage level necessary to achieve a given power transfer level.

Fig. 8

A final statement made in the paper is worth pointing out (*italics added*):

“Any departures from the *assumed performance criteria* and *system parameters* -- which, for convenience, are clearly enumerated on the EHV/UHV loadability chart shown in Figure 8 -- must not be ignored and, depending on their extent, they should properly be accounted for in the line loadability estimates. To illustrate this, the effect of some of the variations in these assumed parameters such as terminal system strength, shunt compensation, line-voltage-drop criterion and stability margin, are investigated in the next section.”

Note from Fig. 8 the “assumed performance criteria”:

- Line voltage drop = 5%
- S-S stability margin = 30%

and the “system parameters”:

- Terminal system S/C – 50 kA (each end)
- No series or shunt compensation →

No series or shunt compensation means distance is an uncompensated distance. If you use series or shunt compensation, voltage (particularly w/ shunt) and stability (particularly w/ series) constraints will be partly alleviated. The model, Fig. 5 above uses  $N$  (series) and  $N_S$ ,  $N_R$  (shunt) to allow for compensation.

The paper provides sensitivity studies on both the performance criteria and some system parameters.

Finally, observe that Fig. 8 also provides a table with

- Nominal voltage
- Number and size of conductors per bundle
- Surge impedance loading
- Line charging per 100 miles

These are “line constant” data! Why do they give them to us?

Although  $P_{\text{rated}}/P_{\text{SIL}}$  is independent of the “line constant” data,  $P_{\text{rated}}$  is not. To get  $P_{\text{rated}}$  from the St. Clair curve, we must know  $P_{\text{SIL}}$ , and  $P_{\text{SIL}}$  very much depends on the “line constant” data.

## 6.0 Resistance

I have posted on the website tables from reference [7] that provide resistance in ohms per mile for a number of common conductors and provided a section of those tables below.

Table 3.3.3																			
CHARACTERISTICS OF MULTILAYER ALUMINUM-CONDUCTOR-STEEL-REINFORCED (ACSR)																			
Code	Cross Section			Stranding		Diameter		L a y e r s	wt lbs per 1000 ft	STRG (Kips)	DC 25 C	Resistance (Ohms/Mile) AC at 60 HZ				GMR (ft)	Reactance 1 ft Rad. 60 HZ		
	(kcmil)	(sq mm)	(sq mm)														X <sub>a</sub> (Ohm/ Mile)	X <sub>a</sub> (Megohm -Mile)	
	Al	Al	Tot	Aluminum	Steel	Cond (in.)	Core (in.)					25 C	50 C	75 C	100 C		(ft)	(Ohm/ Mile)	(Megohm -Mile)
—	2776	1407	1521	84x.1818	19x.1091	2.000	.546	4	3219	81.6	.0338	.0395	.0421	.0452	.0482	.0667	.329	.0736	
Joree	2515	1274	1344	76x.1819	19x.0849	1.880	.425	4	2749	61.7	.0365	.0418	.0450	.0482	.0516	.0621	.337	.0755	
Thrasher	2312	1171	1235	76x.1744	19x.0814	1.802	.407	4	2526	57.3	.0397	.0446	.0482	.0518	.0554	.0595	.342	.0767	
Kiwi	2167	1098	1146	72x.1735	7x.1157	1.735	.347	4	2303	49.8	.0424	.0473	.0511	.0550	.0589	.0570	.348	.0778	
Bluebird	2156	1092	1181	84x.1602	19x.0961	1.762	.480	4	2511	60.3	.0426	.0466	.0505	.0544	.0584	.0588	.344	.0774	
Chukar	1781	902	976	84x.1456	19x.0874	1.602	.437	4	2074	51.0	.0516	.0549	.0598	.0646	.0695	.0534	.355	.0802	

A DC value is given, at 25°C, which is just  $\rho l/A$ , where  $\rho$  is the electrical resistivity in ohm-meters,  $l$  is the conductor length in meters, and  $A$  is the conductor cross-sectional area in meters<sup>2</sup>.

The tables also provide 4 AC values, corresponding to 4 different operating temperatures (25, 50, 75, and 100°C). These values are all higher than the DC value because of the skin effect, which causes a non-uniform current density to exist such that it is greater

at the conductor's surface than at the conductor's interior. This reduces the effective cross-sectional area of the conductor<sup>2</sup>.

Resistance also increases with resistance because temperature increases the level of electron mobility within the material.

## **7.0 General comments on overhead transmission**

In the US, HV AC is considered to include voltage levels 69, 115, 138, 161, and 230 kV.

EHV is considered to include 345, 500, and 765 kV. There exists a great deal of 345 and 500 kV all over the country. The only 765 kV today in the US is in the Ohio and surrounding regions, owned by AEP, as indicated by Fig. 9 [9]. Transmission equipment designed to operate at 765 kV is sometimes referred to as an 800 kV voltage class. There also exists 800 kV-class transmission in Russia, South Africa, Brazil, Venezuela, South Korea, and Quebec.

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<sup>2</sup> Loss studies may model AC resistance as a function of current, where ambient conditions (wind speed, direction, and solar radiation) are assumed.

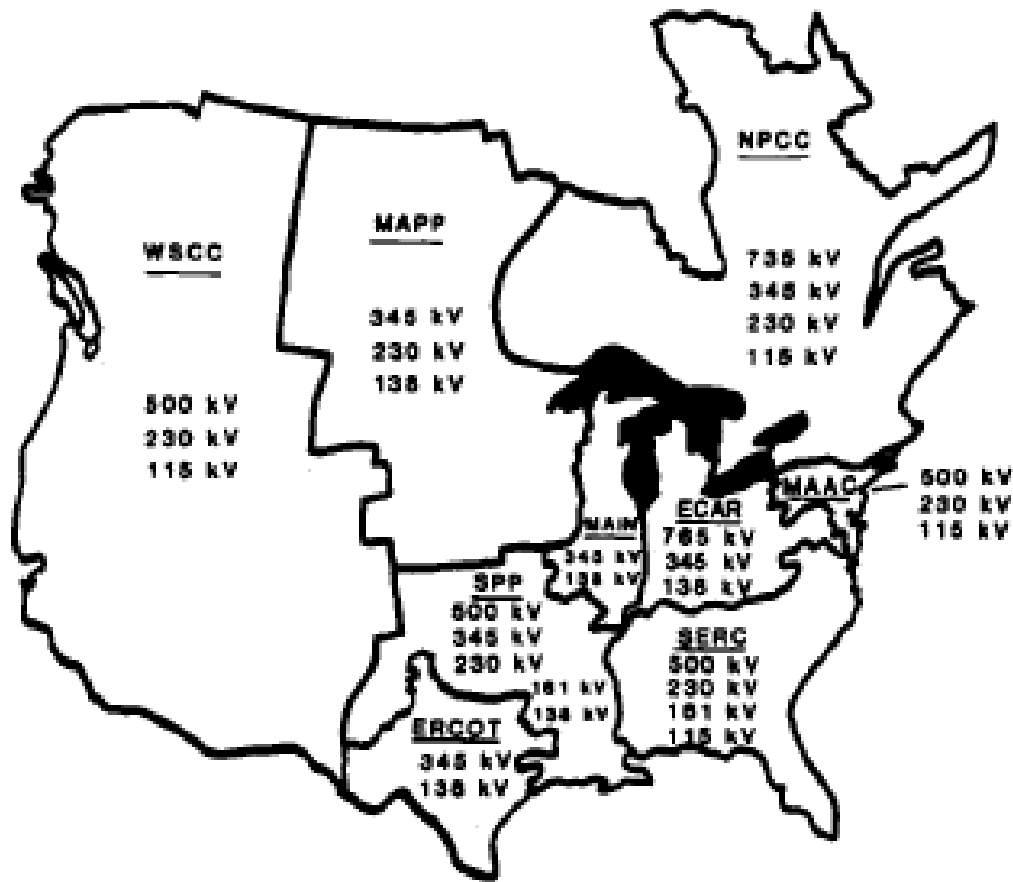


Fig. 9

Figure 10 shows ABB's deliveries of 800 kV voltage class autotransformers (AT) and generator step-up banks (GSUs) from 1965 to 2001 [10].

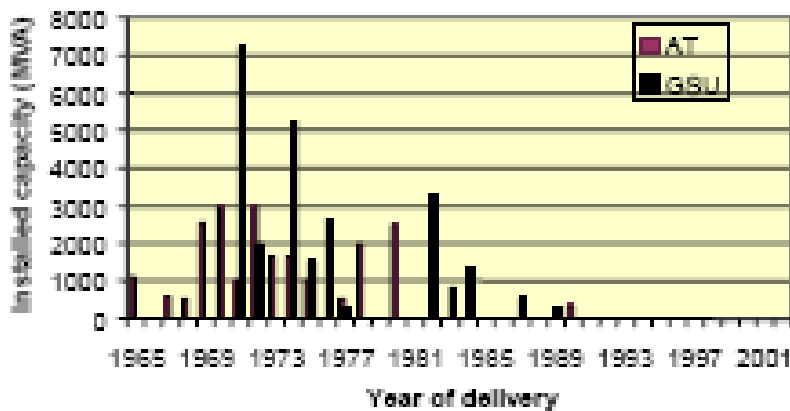


Fig. 10

It is clear from Fig. 10 there was a distinct decline in 765 kV AC investment beginning in early 1980s and reaching bottom in 1989. However, there has been renewed interest in 765 kV during the past few years, with recently completed projects in China & India. I am unaware of 765kV US projects moving forward in the near future.

UHV is considered to include 1000 kV and above. There is no UHV transmission in the US. There was 1200 kV UHV in neighboring countries to Russia [11], and in Japan, but the operational voltage of these lines were downgraded to 500kV. China completed a 1000 kV transmission project in 2009 [12].

## **8.0 General comments on underground transmission**

Underground transmission has traditionally not been considered a viable option for long-distance transmission because it is significantly more expensive than overhead due to two main issues:

- (a) It requires insulation with relatively high dielectric strength owing to the proximity of the phase conductors with the earth and with each other. This issue becomes more restrictive with higher voltage. Therefore the operational benefit to long distance transmission of increased voltage levels, loss reduction (due to lower current for a given power transfer capability), is, for underground transmission,



offset by the significantly higher investment costs associated with the insulation.

- (b) The ability to cool underground conductors as they are more heavily loaded is much more limited than overhead, since the underground conductors are enclosed and the overhead conductors are exposed to the air and wind.

Table 1 [13] provides a cost comparison of overhead and underground transmission for three different AC voltage ranges.

Table 1

<b>Voltage Range</b>	<b>110 - 219kV</b>	<b>220 -362kV</b>	<b>363 -764kV</b>
<b>Mean MVA/circuit</b>	200	600	1800
<b>Mean Overhead Line Cost \$/km/MVA</b>	820	390	185
<b>Mean Underground Cable Cost \$/km/MVA</b>	6100	4900	3700
<b>Mean Cost Ratio</b>	7	13	20
<b>Spread</b>	3.4 -16	5.1 - 21.1	14.6 -33.3

Although Table 1 is dated (1996), it makes the point that the underground cabling is significantly more expensive than overhead conductors.

Note, however, that this issue does not account for obtaining right-of-way. Because underground is not exposed like overhead, it requires less right-of-way. This fact, coupled with the fact that public resistance to overhead is much greater than underground, can bring overall installation costs of the two technologies closer together. This smaller difference may be justifiable, particularly if it is simply not possible to build an overhead line due to public resistance. Such has been the case in France now for several years.

Another issue for underground AC is the high charging currents generated because of the capacitive effect caused by the insulation shield and the conductor. These high charging currents make voltage regulation very difficult for long underground AC transmission, and so typically underground AC is not used beyond a certain length.

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